A FAMILY OF HOLOMORPHIC FUNCTIONS
DEFINED BY DIFFERENTIAL INEQUALITY

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Abstract. The aim of the present paper is to introduce and study a subfamily of holomorphic
and normalized functions defined by a differential inequality. Some geometric properties of
this family of holomorphic functions and different problems of a family of such functions are
presented.

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