

DIFFERENTIAL HARNACK ESTIMATE OF SOLUTIONS TO A CLASS OF SEMILINEAR PARABOLIC EQUATION

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Abstract. In this paper, we obtain a differential Harnack estimate for a semilinear parabolic equation using parabolic maximum principle. As applications of this estimate, we derive blow-up of solutions for this equation and a classical Harnack inequality by integrating along space-time paths.

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