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MULTILINEAR OFF–DIAGONAL LIMITED RANGE EXTRAPOLATIONS

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Abstract. We study the Rubio de Francia's extrapolation theorem. We prove an off-diagonal limited range extrapolation theorem. Using this theorem, we obtain a multilinear off-diagonal limited range extrapolation theorem. Our results generalize and refine known results by Duoandikoetxea (2011), Cruz-Uribe and Martel (2018) and Li, Martell and Ombrosi (2020).

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