

CONTINUOUS SYMMETRIZATION AND CONTINUOUS INCREASING REFINEMENTS OF INEQUALITIES AND MONOTONICITY OF EIGENVALUES

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Abstract. Continuous symmetrization process and continuous increasing process are the tools used in this paper to refine Clausing inequality and Slater-Pečarić inequality. Also, we note on the monotonicity of the first eigenvalue of a Sturm-Liouville system.

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