

## SOME CONVERSES OF FUNCTIONAL HÖLDER–TYPE INEQUALITIES

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*Abstract.* In this paper we obtain some new converses of the Hölder and Minkowski inequalities for positive linear functionals. Our results also provide new converses in case of sums, integrals and time scales integrals. Further we obtain a converse of integral Minkowski's inequality on time scales.

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