

## WEIGHTED COMPOSITION OPERATORS FROM WEIGHTED BERGMAN–ORLICZ SPACES WITH DOUBLING WEIGHTS TO WEIGHTED ZYGMUND SPACES

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*Abstract.* We characterize the boundedness and compactness of weighted composition operators from weighted Bergman-Orlicz spaces with doubling weights to weighted Zygmund spaces on the unit disc.

*Mathematics subject classification (2020):* 30H99, 47B33.

*Keywords and phrases:* Weighted composition operator, Bergman-Orlicz space, weighted Zygmund space, doubling weight.

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