MONOTONICITY OF RATIOS OF BERNOULLI POLYNOMIALS

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Abstract. Monotonicity patterns of the ratios B_k/B_{k+2} of Bernoulli polynomials are determined.

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