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BOUNDARY VALUES OF SEQUENCES AT INFINITY IN DIFFERENCE SPACES OF THE SOBOLEV TYPE

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Abstract. Weighted difference Sobolev space $W^n_{p,\upsilon}$ is determined. The mutual relation of this space with the space $\overset{\circ}{W}{}^n{}_{p,\upsilon}$ is investigated depending on the behavior of the weight sequences at infinity.

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