

## SPECTRAL CONTINUITY OF $k$ -TH ROOTS OF HYPONORMAL OPERATORS

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*Abstract.* Continuity of the set theoretic function spectrum, and some of its distinguished parts, on the class of  $k$ -th roots of hyponormal operators is proved.

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