

STABILITY OF QUADRATIC PROJECTION METHODS

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Abstract. We discuss stability properties of the method studied recently in [7] and [2], for computing eigenvalues in gaps of the essential spectrum of self-adjoint operators.

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