PROJECTIONS AND THE KADISON–SINGER PROBLEM

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Abstract. We prove some new equivalences of the paving conjecture and obtain some estimates on the paving constants. In addition we give a new family of counterexamples to one of the Akemann-Anderson conjectures.

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