UNITARY EQUIVALENCE TO A COMPLEX SYMMETRIC MATRIX: GEOMETRIC CRITERIA

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Abstract. We develop several methods, based on the geometric relationship between the eigenspaces of a matrix and its adjoint, for determining whether a square matrix having distinct eigenvalues is unitarily equivalent to a complex symmetric matrix. Equivalently, we characterize those matrices having distinct eigenvalues which lie in the unitary orbit of the complex symmetric matrices.

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