JORDAN LEFT DERIVATIONS AND SOME LEFT DERIVABLE MAPS

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Abstract. Let $\mathscr{A}$ be an algebra and $\mathscr{M}$ be a left $\mathscr{A}$-module. We say that a linear mapping $\varphi : \mathscr{A} \to \mathscr{M}$ is a left derivable mapping at P if $\varphi(ST) = S\varphi(T) + T\varphi(S)$ for any $S, T \in \mathscr{A}$ with $ST = P$. In this paper, we show that Jordan left derivations or left derivable mappings at zero or unit on some algebras are zero under certain conditions.

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