UNBOUNDED OPERATORS COMMUTING WITH THE
COMMUTANT OF A RESTRICTED BACKWARD SHIFT

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Abstract. It is shown that, in a proper coinvariant subspace of the shift operator on the Hardy space H^2, a densely defined operator that commutes with the commutant of the restricted backward shift is closable. A connection between this result and a case of the transitive algebra problem is discussed.

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