

PAVING SMALL MATRICES AND THE KADISON–SINGER EXTENSION PROBLEM

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Abstract. We compute paving parameters for classes of small matrices and the matrices that yield them. The convergence to 1 or not of the sequence of these parameters is equivalent to the Kadison-Singer Extension Problem.

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