

## A CONDITIONAL EXPECTATION TYPE OPERATOR ON $L^p$ SPACES

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*Abstract.* In this paper we discuss some of the basic operator-theoretic characterizations for conditional expectation type operator  $T = EM_u$  on  $L^p$  spaces.

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