

## ALGEBRAS OF TRUNCATED TOEPLITZ OPERATORS

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*Abstract.* We find necessary and sufficient conditions for the product of two truncated Toeplitz operators on a model space to itself be a truncated Toeplitz operator, and as a result find a characterization for the maximal algebras of bounded truncated Toeplitz operators.

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