Operators and Matrices
Volume 5, Number 3 (2011), 505–510

THE DENSITY OF THE RANGE OF $X \mapsto AX - XB$ WITH A, B^* M–HYPONORMALS

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Abstract. We extend a result of L. A. Fialkow concerning the density of the range and the injectivity of the operator $X \mapsto AX - XB$ with A, B^* M-hyponormal operators with no holes in the essential spectrum of negative Fredholm index.

Mathematics subject classification (2010): 47B20.
Keywords and phrases: Generalized derivations, hyponormal operators, density of the range.

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Paper OaM-05-38