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# QUASILINEAR MAPPINGS, $M$–IDEALS AND POLYHEDRA

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*Abstract.* We survey the connection between two results from rather different areas: failure of the 3-space property for local convexity (and other properties) within the category of quasi-Banach spaces, and the irreducibility (in the sense of Minkowski difference) of large families of finite dimensional polytopes.

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