ON HILBERT–SCHMIDT COMPATIBILITY

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Abstract. Guided by important examples of differential operators, we obtain sufficient conditions for Hilbert-Schmidt compatibility of operators and apply these conditions in spectral perturbation theory.

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