

WEAK MAJORIZATION INEQUALITIES FOR SINGULAR VALUES

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Abstract. In this paper, we refine an inequality due to Bhatia and Kittaneh [Linear Algebra Appl. 308 (2000) 203–211], and generalize another inequality by Bhatia and Kittaneh [Lett. Math. Phys. 43 (1998) 225–231].

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