

ESSENTIAL NORM OF GENERALIZED COMPOSITION OPERATORS ON WEIGHTED HARDY SPACES

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Abstract. Upper and lower bounds for the essential norm of generalized composition operators on weighted Hardy spaces are estimated.

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