GREEN'S FUNCTION, RESOLVENT, PARSEVAL EQUALITY OF DIFFERENTIAL OPERATOR WITH BLOCK–TRIANGULAR MATRIX COEFFICIENTS

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Abstract. Green's function for the Sturm-Liouville operator with a block-triangular matrix potential growing at infinity is constructed. For this function, a series expansion is obtained and the Parseval equality is proved.

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