COMMUTING OF BLOCK DUAL TOEPLITZ OPERATORS

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Abstract. In this paper, we characterize the commuting (semi-commuting) and the essentially commuting (semi-commuting) of block dual Toeplitz operators.

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