

A SIMPLE SUFFICIENT CONDITION FOR COMPLETE POSITIVITY

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Abstract. We use row sums and rank to give a sufficient condition on the diagonal entries of a doubly nonnegative matrix for it to be completely positive and its cp-rank equal to its rank.

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