

FRAMES AND OPERATORS IN HILBERT C^* -MODULES

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Abstract. In this paper we introduce the concepts of atomic systems for operators and K -frames in Hilbert C^* -modules and we establish some results.

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