

## SOME RESULTS ON ABSOLUTE CONTINUITY FOR UNBOUNDED JACOBI MATRICES

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*Abstract.* This brief paper presents several results which offer a useful approach for studying the absolute continuity of spectral measures associated with some Jacobi matrix operators. The operators are modeled as multiplication operators on a dense domain of a function space with a polynomial basis. Properties of these polynomials and commutator equations are used to obtain results on absolute continuity.

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