

SPECTRA OF INFINITE GRAPHS VIA SCHUR COMPLEMENT

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Abstract. The goal of the paper is to apply the general operator theoretic construction known as the Schur complement for computation of the spectrum of certain infinite graphs which can be viewed as finite graphs with rays attached to them. The examples of a multiple star and a flower with infinite rays are considered.

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