COMPLEX SYMMETRIC OPERATORS ACTING
BETWEEN TWO DIFFERENT HILBERT SPACES

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Abstract. This paper will initiate a study on the class of complex symmetric operators acting between two different Hilbert space. Among other things, we compute the closure of CSO_u and CSO_b with respect to the several topologies.

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