SECOND REGULARIZED TRACE OF A DIFFERENTIAL OPERATOR WITH SECOND ORDER UNBOUNDED OPERATOR COEFFICIENT GIVEN IN A FINITE INTERVAL

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Abstract. In this work, we establish a formula for the second regularized trace of a second order differential operator with unbounded operator coefficient given in a finite interval.

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