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OPERATOR–VALUED MAPS ON HILBERT C^*–MODULES

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Abstract. We provide a characterization for operator-valued completely bounded linear maps on Hilbert C^*-modules in terms of φ-maps. Also, we show that for every operator-valued completely positive map φ on a C^*-algebra $\mathscr{A}$, there is a unique (up to multiplication by a unitary operator) non-degenerate φ-map on each Hilbert $\mathscr{A}$-module.
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