

DILATIONS SIMILAR TO A SELF-ADJOINT OPERATOR

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Abstract. It is shown that every bounded linear operator T in a complex Hilbert space H is the $(1, 1)$ -compression of an operator in $H \oplus H$ that is similar to a self-adjoint operator.

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