

ON THE OPEN BALL CENTERED AT AN INVERTIBLE ELEMENT OF A BANACH ALGEBRA

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Abstract. Let A be a complex unital Banach algebra. Since the set of invertible elements is open, there is an open ball around every invertible element. In this article, we investigate the Banach algebras for which the radius given by the Neumann series is optimal.

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