

SOME SPECTRAL PROPERTIES OF FOURTH ORDER DIFFERENTIAL OPERATOR EQUATION

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Abstract. We consider boundary value problem for fourth order differential equation with unbounded discrete operator coefficient. One of the boundary conditions involves the λ parameter. The asymptotics of spectrum of corresponding selfadjoint operator is obtained. We also calculate the trace of that operator.

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