

## NORMS OF HYONORMAL WEIGHTED COMPOSITION OPERATORS ON THE HARDY AND WEIGHTED BERGMAN SPACES

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*Abstract.* In this paper, first we find norms of hyponormal weighted composition operators  $C_{\psi, \varphi}$ , when  $\varphi$  has a Denjoy-Wolff point on the unit circle. Then for  $\varphi$  which is analytic self-map of  $\mathbb{D}$  with a fixed point in  $\mathbb{D}$ , we investigate norms of hyponormal weighted composition operators  $C_{\psi, \varphi}$ .

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