

WEYL'S THEOREM AND ITS PERTURBATIONS FOR THE FUNCTIONS OF OPERATORS

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Abstract. In this paper, we study the stability of Weyl's theorem under compact perturbations, and characterize those operators satisfying that the stability of Weyl's theorem does not hold for any integer powers of the operator.

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