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SELF–COMMUTATOR NORM OF HYPONORMAL TOEPLITZ OPERATORS

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Abstract. Chu and Khavinson recently obtained a lower bound for the norm of the self-commutator of a certain class of hyponormal Toeplitz operators on the Hardy space. Via a different approach, we offer a generalization of their result.

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