

## COMPACT PERTURBATIONS OF DRAZIN INVERTIBLE OPERATORS

BOTING JIA AND YOU Ling FENG

*Abstract.* Necessary and sufficient conditions for the invariance of Drazin invertibility under compact perturbations are established. This proves a conjecture of Kaifan Yang and Hongke Du.

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