

## SIMILARITY JORDAN MULTIPLICATIVE MAPS

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*Abstract.* We characterize bijections  $\phi : B(X) \rightarrow B(X)$  satisfying that  $\phi(AB + BA)$  and  $\phi(A)\phi(B) + \phi(B)\phi(A)$  are similar for all  $A, B \in B(X)$ .

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