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A NOTE ON THE MAXIMAL NUMERICAL RANGE

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Abstract. We show that the maximal numerical range of an operator has a non-empty intersection with the boundary of its numerical range if and only if the operator is normaloid. A description of this intersection is also given.

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