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SOME INEQUALITIES INVOLVING POSITIVE LINEAR MAPS UNDER CERTAIN CONDITIONS

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Abstract. We demonstrate that several well-known classical inequalities also hold for some positive linear maps on matrix algebra. It is shown that for such maps the Jensen inequality hold for all ordinary convex functions.

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