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ON MAPS SENDING RANK–κ IDEMPOTENTS TO IDEMPOTENTS

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Abstract. We characterize bijective linear maps on complex-valued $n \times n$ matrices such that rank-κ idempotents are mapped to idempotents, where $2 \leqslant \kappa < n-1$.

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