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LYAPUNOV PROPERTY OF POSITIVE C_0–SEMIGROUPS ON NON–COMMUTATIVE L^p SPACES

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Abstract. That the growth bound of a positive C_0-semigroup on classical L_p-space coincides with the spectral bound of its generator, is a well known result in classical semigroup theory. In this paper we study this result in the non-commutative setting.

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