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MEASURES OF NONCOMPACTNESS IN $\bar{N}(p,q)$ SUMMABLE SEQUENCE SPACES

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Abstract. In this paper, we first define the $\bar{N}(p,q)$ summable sequence spaces and obtain some basic results related to these spaces. The necessary and sufficient conditions for an infinite matrix A to map these spaces into the spaces c_0, c and ℓ_∞ is obtained and Hausdorff measure of noncompactness is then used to obtain the necessary and sufficient conditions for the compactness of linear operators defined on these spaces.

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