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ON EXTENSIONS OF SYMMETRIC OPERATORS

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Abstract. We give an explicit description of all minimal self-adjoint extensions of a densely defined, closed symmetric operator in a Hilbert space with deficiency indices $(1,1)$.

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