

SOME NEW OPERATOR INEQUALITIES

MOHAMMAD SABABHEH, HAMID REZA MORADI AND IBRAHIM HALIL GÜMÜŞ

Abstract. In this article, we present some new inequalities for positive linear mappings that can be viewed as super multiplicative inequalities. As applications, we deduce some numerical radius inequalities. Then several inequalities for the numerical radius are presented with the aid of convex functions.

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