

A NOTE ON ORLICZ ALGEBRAS

SEYYED MOHAMMAD TABATABAIE, ALI REZA BAGHERI SALEH AND
MARYAM ZARE SANJARI

Abstract. The purpose of this paper is to give a necessary and sufficient condition for an Orlicz space $L^\Phi(G)$ to be a convolution Banach algebra, where G is a compactly generated locally compact abelian group and Φ is a Young function satisfying Δ_2 -condition and an extra sequence condition.

Mathematics subject classification (2010): 46E30, 43A15.

Keywords and phrases: Locally compact group, Orlicz algebra, convolution, Young function, N-function, Zygmund space.

REFERENCES

- [1] F. ABTAHI, R. NASR ISFAHANI AND A. REJALI, *On the L_p -conjecture for locally compact groups*, Arch. Math. (Basel) **89**, (2007), 237–242.
- [2] C. CHEN AND C.-H. CHU, *Hypercyclic weighted translations on groups*, Proc. Amer. Math. Soc. **139**, (2011), 2839–2846.
- [3] E. HEWITT AND K. A. ROSS, *Abstract Harmonic Analysis*, Springer-Verlag, Heidelberg, 1979.
- [4] H. HUDZIK, A. KAMISKA AND J. MUSIELAK, *On some Banach algebras given by a modular*, in: Alfred Haar Memorial Conference, Budapest, Colloquia Mathematica Societatis János Bolyai (North Holland, Amsterdam), **49**, (1987) 445–463.
- [5] M. M. RAO AND Z. D. REN, *Theory of Orlicz Spaces*, Marcel Dekker, New York, 1991.
- [6] A. OSANÇLIOL AND S. ÖZTOP, *Weighted Orlicz algebras on locally compact groups*, J. Aust. Math. Soc. **99**, (2015), 399–414.
- [7] K. URBANIK, *A proof of a theorem of Zelazko on L^p -algebras*, Colloq. Math. **8**, (1961), 121–123.
- [8] W. ZELAZKO, *A note on L^p -algebras*, Colloq. Math. **10**, (1963), 53–56.