THE SPECTRUM OF THE RESTRICTION TO AN INVARIANT SUBSPACE

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Abstract. Let X be a Banach space, $A \in B(X)$ and M be an invariant subspace of A. We present an alternative proof that, if the spectrum of the restriction of A to M contains a point that is in any given hole in the spectrum of A, then the entire hole is in the spectrum of the restriction.

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