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QUANTIZATION OF $A_0(K)$–SPACES

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Abstract. Let $(V,\{\|.\|_n\},\{M_n(V)^+\})$ be a C^*-ordered operator space and $Q_n(V)$ be the quasi-state space of $M_n(V)$. We show that every C^*-ordered operator space V is complete isometrically, completely isomorphic to $\{A_0(Q_n(V),M_n(V^*))\}$. Motivated by this result we study matricial convexity property. We introduce a notion of an L^1-matrix convex set $\{K_n\}$ in a $*$-locally convex space X. We show that every quantized function space $\{A_0(K_n,M_n(X))\}$ is a C^*-ordered operator space. Further, we generalize the notion of regular embedding of a compact convex set to L^1-regular embedding of an L^1-matrix convex set. We show that if a L^1-matricial convex set is L^1-regular embed and L^1-matricial cap, then $A_0(K_n,M_n(V))$ is an abstract operator system.

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