Operators and Matrices
Volume 14, Number 4 (2020), 951–958
doi:10.7153/oam-2020-14-59

SEMI–SMOOTH POINTS IN SPACE OF OPERATORS ON HILBERT SPACE

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Abstract. The investigations of the smooth points in the operator spaces $\mathscr{K}(\mathscr{H})$ and $\mathscr{L}(\mathscr{H})$ were started in [J. R. Holub, Math. Ann. **201** (1973), 157–163] and [T. J. Abatzoglou, Math. Ann. **239** (1979), 129–135]. The aim of this paper is to present a description of semi-smooth points in the operator spaces $\mathscr{L}(\mathscr{H}_1,\mathscr{H}_2)$ and $\mathscr{K}(\mathscr{H}_1,\mathscr{H}_2)$.

Mathematics subject classification (2010): 46B20, 46B28, 46C50, 47L05.
Keywords and phrases: Hilbert space, space of operators, norm derivatives, semi-smoothness.

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Paper OaM-14-59